

A theoretical calculation of relative pKas of phosphonic acids in an aqueous solution using idodesmic reaction and the Polarisable Continuum Model

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ABSTRACT: The geometries of the neutral and deprotonated structures of 24 phosphonic acids *R-PO*₃*H*₂ are optimized at the HF and B3LYP level using $6-31^{++}G^{**}$ and LANL2DZ basis set and SMD solvation model (R=H, CH₃, C₂H₅, n-C₃H₇, n-C₄H₉, n-C₆H₁₃, iso-C₃H₇, iso-C₄H₉, s-C₄H₉, t-C4H9, CH2CH(CH3)3, C(CH3)2C2H5, CH2C6H5, CH=CH2, CH=CHC6H5, C6H5, CH2OH, CF3, CH₂Cl, CHCl₂, CCl₃, CH₂Br, CH₂I, and CH₂Si(CH₃)₃). Relative pka₁ and pka₂ of these systems are then calculated at the same level by isodesmic reaction in aqueous phase. The calculated values of the pKas are compared to the corresponding experimental values. The average error of pKas varies between -1.62 ± 1.92 and -0.01 ± 1.28 pKa unit. The correlations are linear and quite high between calculated pKas ($0.92 \le R^2 \le 0.99$) and calculated pKas versus experimental ones $(0.73 \le R^2 \le 0.91)$. In addition, the experimental pka₁ values of phosphonic acids are scaled by comparison with the pKa of corresponding carboxylic acids. The scaled pkal values made it possible to improve the correlation between the experiment and the theory ($0.91 \le R^2 \le 0.97$). This study shows that the calculations of the relative dissociation constant pKa of phosphonic acid derivatives via isodesmic reaction at the HF and B3LYP level using the bases $6-31^{++}$ G^{**} and LANL2DZ with the solvation model SMD conduct to results with a precision of better quality. KEYWORDS: Deprotonation, isodesmic reaction, pKa dissociation constant, SMD solvation model, Phosphonic Acid

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I. INTRODUCTION

Phosphonic acids constitute a special class of molecules within phosphorus-containing compounds. The tetrahedral P atom is connected via a P=O double bond to O, while it forms two P-O single bonds with OH groups. The P atom also has a single bond with carbon (P-C), the latter originating from an aliphatic or aromatic fragment R.The phosphonic acid group exhibits variable acidity.



Figure 1: chemical formula and deprotonation processes in the phosphonic acids.

There are two stepwise deprotonation processes, as shown in Figure 1. It should be noted that these deprotonation reactions are feebly studied. Only a few determinations of dissociation constants of some phosphonic acids are recorded in literature (P. Nylen, 1930)(P. Rumpf1947) (J. R. White, 1950)(Crofts, P. C., 1953). The purpose of the latest investigation of Crofts et al. was the study of the effects of variations within the alkyl group of the acids on the apparent dissociation constants of these acids.

The measured apparent dissociation constants values are shown in Table 1(appendix). The range of variation of pKa_1 [1.3 to 3.48] and that of pKa_2 [3.93 to 8.48] is broad and provides an opportunity for a statistical analysis of the substitution effect on the acidity of phosphonic acids. Therefore, it is interesting to study the deprotonation reactions of



Figure 2: chemical formula of phosphonic acids.

phosphonic acids derivatives using computational chemistry.

In this work, our objective is to enrich the literature with more accurate data of dissociation constants pKa values of these compounds. The substituent effect analysis will be the subject of a next paper. The schematic structures of some phosphonic acids selected shown in Figure 2.

II. COMPUTATIONAL METHODS AND PROCEDURES

2.1 Acidity pKa constants

The phosphonic acid R-PO₃H₂, noted AH₂ is a weak diacid. It dissociates in water following the reactions (1a) and (1b):

$$AH_{2(aq)} \leftrightarrow AH_{(aq)} + H_{(aq)}^{+}$$
 [1a]

$$AH^{-}_{(aq)} \leftrightarrow A^{2-}_{(aq)} + H^{+}_{(aq)}$$
 [1b]

Equations (1a) and (1b) are respectively characterized by the equilibrium constants denoted Ka1 and Ka2:

$$Ka_{1} = \frac{[AH_{(aq)}^{-}]*[H_{(aq)}^{+}]}{[AH_{2(aq)}]}$$
[2a]
$$Ka_{2} = \frac{[A_{(aq)}^{-}]*[H_{(aq)}^{+}]}{[AH_{(aq)}]}$$
[2b]

pKa_i(i=1 or 2) is defined as:

$$pk_{ai} = -\log Ka_i = \frac{\Delta G^*_{i(aq)}}{2.303 \text{RT}}$$
[3]

 $\Delta G_{i(aq)}^*$ is the Gibbs free energy of the dissociation reaction, R is the ideal gases constant (R=1.987.10⁻³kcal.mol⁻¹.K⁻¹) and T is the absolute temperature in Kelvin (T=298.15K).

The computation of acid dissociation constants is a demanding and arduous process because an error of 1.36 kcal/moll in the change of free energy of reaction 1a or 1b results in an error of 1 pKa unit (Liptak, 2001),(Liptak, 2002).

Therefore, to optimize errors, the pK_{ai} relative acidity constants are evaluated with respect to that of a reference system BH_2 according to the isodesmic reaction pathway (4). The reference system BH_2 chosen and used here is the phosphonic acid H-PO₃H₂. The choice is based on its chemical structure, which is similar to the studied compounds and the fact offers the possibility of quantifying the substituent effects on the acidity constants

2. 2 Computational details

2.2.1 The calculation levels

All calculations have been carried out on 24 phosphonic acid compounds using the Gaussian 16 software (M. J. Frisch, 2016), at Hartree-Fock (HF), density functional theory (DFT) using Becke's three parameter (B3) exchange and the Lee–Yang–Parr (LYP) correlation functional (Becke AD, 1993). (Lee C, 1988). (Miehlich B, 1989) and AM1 level(M. J. S. Dewar, 1977) (M. J. S. Dewar, 1985).

The $6-31^{++}G(d,p)$ Pople-type basis sets(P. C. Hariharan, 1974) (P. C. Hariharan, 1973), and LanL2DZ pseudopotential basis sets (Hay,1985) (T. H. Dunning Jr, 1976) (W. R. Wadt,1985) (P. J. Hay,1985) integrated in Gaussian 16 were used. The use of polarization and diffuse OAs is justified by the presence of negative charges and intramolecular hydrogen bonding in deprotonated systems. The solvation energies were obtained at the same theory levels using the SMD model(V. Barone, 1998) (M. Cossi, 2003) (Marenich, 2009).

2.2.2 Geometry optimization

The HF and DFT calculations were performed using the gas phase starting geometries obtained with the AM1 semi empirical method (Dewar, 1977) (Dewar, 1985). Thereafter, the scanning of the potential energy surface was carried out for the $(OH)_2P=Oand$ the CX group together by the variation of each dihedral angle D1, D2 and D3 of 0° to 360° with a step of 10° Figure 3.



2.2.3 Gibbs free energy calculation

The proton exchange reaction is a process in which the proton liberated by the acid $AH_{i(aq)}^{p}$ is fixed by the reference base $BH_{i-1(aq)}^{p-1}$ according equations [4]:

$$AH_{i(aq)}^{p} + BH_{i-1(aq)}^{p-1} \stackrel{\Delta G_{aq}^{\circ}}{\longleftrightarrow} AH_{i-1(aq)}^{p-1} + BH_{i(aq)}^{p}[4]$$

Where p and p-1 represent the global charge of the acid species and its conjugate base respectively for i=2 first dissociation and p=0 and i=1, p=-1 second dissociation.

The $\Delta G^*_{i(aq)}$ free energy reaction is determined according Equation (5):

$$\Delta G_{i(aq)}^{*} = G_{aq}^{*}(AH_{n-1(aq)}^{p-1}) + G_{aq}^{*}(BH_{n(aq)}^{p}) - G_{aq}^{*}(AH_{n(aq)}^{p}) - G_{aq}^{*}(BH_{i-1(aq)}^{p-1})$$
[5]

The geometrical optimization and the calculation of the frequencies of the reactants and products in solution allow determining the standard free energy $G_{aq}^*(X_{(aq)})$ at 298.15K.

III. RESULTATS AND DISCUSSION

The calculated acid dissociation constant pKa values for 24 phosphonic acids obtained as described above are compared with the experimental values identified in literature table 1 (appendix). Also, the average value of pKa calculated at different levels is carried with the standard deviation for comparison. The obtained pKa values are usually in the order of magnitude of the corresponding experimental values except 18, 19, 20, and 21 compounds. The latter have significant pKa₁ negative values at the HF and B3LYP levels. Table 2 (appendix) shows the errors of calculated pKa values relative to experimental one and table 3 illustrates the statistical parameters concerning some errors. The SMD-HF and SMD-B3LYP methods overestimate or underestimate the pKa values of the phosphonic acids studied. The maximum positive error is 2.50 pKa, while the negative error is quite high at -9.45 pKa. These two values are obtained with the method of B3LYP / LANL2DZ. The mean signed error MSE values are between -0.01±1.28 and -1.62±1.92 pKa unit. The values of these means become equal to -0.19 ±1.39 and -0.90 ±1.69 pKa units respectively without the 18, 20 and 21 compounds which have a large negative error. The mean unsigned error MUE values are 0.51±0.76 and 1.69±1.69 pKa units respectively. The MSE values of $\Delta pKa_1\Delta pKa_2$ (mean value) are respectively -0.84±2.41 and -0.67±1.57 and strongly

Table 3. Statistical parameters: Mean Signed Errors (MSE), Mean Unsigned Errors (MUE) and Standard
Deviation (SD) in pKa's of phosphonic acids calculated at SMD-HF and SMD-B3LYP level (N=21 for 6-
$21 + C^{**}$ and N=22 for LANI 2DZ basis set

31++G ^{**} and N=23 lot LANL2DZ basis set).									
		MSE	MUE	SD					
HF/B1	pKa ₁	-0.47	1.56	2.31					
	pKa_2	-0.17	0.83	1.22					
HF/B2	pKa ₁	-1.11	1.6	2.26					
	pKa ₂	-0.01	0.89	1.28					
B3LYP/B1	pKa1	-0.06	1.64	2.26					
	pKa ₂	-1.15	1.96	2.18					
B3LYP/B2	pKa ₁	-1.6	1.76	2.7					
	pKa ₂	-1.62	2.03	1.92					
Mean Value	pKa ₁	-0.84	1.48	2.41					
	pKa_2	0.67	1.12	1.57					
Whitout compound 18	3, 20 and 21.								
HF/B1	pKa ₁	0.4	0.86	1.21					
	pKa_2	0.26	0.51	0.76					
HF/B2	pKa ₁	-0.19	0.75	1.39					
	pKa ₂	0.35	0.66	0.99					
B3LYP/B1	pKa ₁	0.79	1.05	1.21					
	pKa_2	-0.45	1.29	1.5					
B3LYP/B2	pKa ₁	0.64	0.83	1.33					
	pKa ₂	-0.9	1.6	1.69					
Mean Value	pKa1	0.02	0.63	1.24					
	pKa ₂	-0.15	0.66	0.95					

reduced to 0.02 ± 1.24 and 0.15 ± 0.95) without the compounds 18, 20 and 21. The MUE values are also reduced to 0.63 ± 1.24 and 0.66 ± 0.95 for $\Delta pKa_1, \Delta pKa_2$ (mean value). These results, obtained without the explicit use of water molecules, are in the order of magnitudes of the values obtained by (Bishnu. T, 2016) in the case of pKa calculations of thiols with three water molecules via the use of SMD-SMD B3LYP / $6-311^{++}G'(d, p)$. In design, the large errors recorded for compounds 18, 19, 20 and 21 and others are probably due to the difficulties of experimental measurements or to the calculation methods used or to both. Asidefrom taking experimental measurements of pKa for phosphonic acids, there is a way to correct these errors and give more reliable pKa values for these compounds. The method is modeling via linear regression analysis where Y is pKa response variable, X is pKa prediction variable, A and B are fitting parameters:

In the following, are presented and discussed, X is pKa prediction variable, A and B are fitting parameters:

$$Y = (A \pm \Delta A) + (B \pm \Delta B) * X)$$
 [6]

In the following, it is presented and discussed, the results of the relations between calculated vs. calculated pKa values and those of calculated vs. experimental.

3.2 Correlation of theory-theory

Table 4 lists the statistical parameters of linear regressions established. The R^2 values are 0.92, 0.99 and SD 0.29, 0.89 pKa units indicating a best correlation theory – theory.

Figure 4 and 5, shows a linear correlation between the calculated pKa at the HF and B3LYP level using the bases $6-31^{++}G^{**}$ and LANL2DZ.

Table 4. Statistical Parameters of Linear Correlations calculated pKa vs calculated pKa of phosphonic acids: $Y=(A\pm\Delta A) + (B\pm\Delta B)*X$; Correlation coefficient R²; standard deviation SD

	Y vs X	$A \pm \Delta A$	$B{\pm}\Delta B$	\mathbb{R}^2	SD
	HF/B2 vs HF/B1.	-0,93±0.19	1,12±0.06	0,95	0,74
	B3LYP/B1vs HF/B1.	0,45±0.08	0,98±0.02	0,99	0,29
a	B3LYP/B2 vs HF/B1	-1,41±0.16	1,15±0.05	0,97	0,63
pK	B3LYP/B1 vs HF/B2.	1,31±0.18	0,82±0.05	0,93	0,76
	B3LYP/B2 vs HF/B2.	-0,48±0.11	1,00±0.03	0,98	0,49
	B3LYP/B2 vs B3LYP/B1.	-1,91±0.21	1,16±0.06	0,95	0,74
	HF/B2 vs HF/B1.	0,41±0.41	0,97±0.05	0,94	0,57
	B3LYP/B1 vs HF/B1.	-3,60±0.52	1,36±0.07	0,95	0,73
.a2	B3LYP/B2 vs HF/B1	-3,42±0.54	1,24±0.07	0,94	0,76
pK	B3LYP/B1 vs HF/B2.	-3,62±0.50	1,25±0.07	0,95	0,69
	B3LYP/B2 vs HF/B2.	-3,91±0.52	1,36±0.07	0,92	0,89
	B3LYP/B2 vs B3LYP/B1.	0,10±0.30	0,90±0.04	0,96	0,64

The slope values of pKa1 and pKa2 are close to unity varying from 0.82 ± 0.05 to 1.16 ± 0.06 pKa1 and from 0.90 ± 0.04 to 1.36 ± 0.07 pKa2. As for the intercept values, they vary in a range of -1.91 ± 0.2 to 1.31 ± 0.18 and -3.91 ± 0.52 , 0.41 ± 0.41 for pKa₁ and pKa₂ respectively.

The slight variation of the slope (increase or decrease with respect to the unit) is probably due to underestimation of solvation energy of the conjugate bases of phosphonic acids by the SMD salvation model.

Table 5. Statistical Parameters of Linear Correlations calculated mean vs experiment of pKa1 and pKa2 dissociation constants of phosphonic

Y	$A \pm \Delta A$	$B\pm \Delta B$	\mathbb{R}^2	SD	Without
HF/B1	-2.79±0.22	2.40 ± 0.22	0.89	0.44	14, 18, 20, 21.
HF/B2	-1.71±0.71	1.83 ± 0.30	0.73	0.60	14, 19, 20, 21, 23, 24.
B3LYP/B1	-2.59 ± 0.48	$2,49 \pm 0.20$	0.91	0.40	14, 18, 20, 21
B3LYP/B2	-1.97±0.56	1.70 ± 0.24	0.78	0.48	14, 18, 20, 21, 23, 24.
HF/B1	-5.10±1.06	1.65 ± 0.14	0.88	0.84	16.
HF/B2	-4.91±1.06	1.64 ± 0.14	0.87	0.86	16.
B3LYP/B1	-10.45±1.75	2.23 ± 0.23	0.84	1.39	16.
B3LYP/B1	-8.80 ± 1.72	1.95 ± 0.20	0.82	1.30	23.



Figure 5: Linear correlation of calculated pKa₁ and pKa₂ value's at HF and B3LYP using 6-31⁺⁺G** and LANL2DZ basis set with PCM-SMD method of phosphonic acid derivatives.

-4

-2

0

pka, (B3LYP/6-31++G**)

2

4

0

2

-2

-4

4

pka, (B3LYP/6-31++G**)

6

8

10

3.3 Correlation of theory-experimental

In order to establish a prediction model for pKa of phosphonic acids, the pKa values calculated at the HF and B3LYP level and their mean values are correlated with the experimental ones available in the literature. The statistical analysis data are summarized in Table 5and correlation lines are plotted on Figure 6.

The coefficient R^2 of 0.8 to 0.9 with a SD of 0.4 to 0.6 pKa unit indicate a good correlation theory vs experience. However, it should be noted that R^2 =0.73 is relatively low in the case of calculation HF/ LANL2DZ. Moreover, the results show the effect of the AO's basis on the parameters A and B. Compared to the all-electron base 6-31⁺⁺ G^{**}, the pseudo-potential baseLANL2DZ decreases the slope of the correlation line of 0.60 at the HF level and 0.80 at the B3LYP level in the case of pKa₁, whereas these variations are quite small in pKa₂0.01 and 0.26. The relatively small variations between the HF and DFT values + 0.09 for 6-31⁺⁺G^{**} and -0.13 for LANL2DZ indicates an insignificant correlation electronic effect on the pKa values.



Figure 6. Linear correlation of experiment pKa1 and pKa2's dissociation constants versus calculated values at HF and B3LYP using 6-31⁺⁺G^{**} and LANL2DZ basis set with PCM-SMD method of phosphonic acid derivatives

The intercept is 1.04 for HF and 0.62 for B3LYP in pKa₁ and 0.19 forHF and 1.65 for B3LYP in pKa₂. Moreover, compounds 14, 16, 18, 19, 20, 21, 23 and 24 have wide residues (X-X ') or (Y-Y') (X 'and Y' are the coordinates of the compound concerned on the correlation line). The difference is due to a strong overestimation or underestimation of the calculated or experimental pKa value or both.

Table 6 shows the statistical parameters of a linear correlation between the calculated means (HF, DFT) and the experimental values of pKa1 and pKa2 of the phosphonic acids. It is found that the coefficients of correlation $R^2 = 0.91$ and $R^2 = 0.86$ for pKa1 and pKa2 respectively, the most very weak deviations standard equal to 0.8 and 0.78 for pKa1 and pKa2 respectively.

 Table 6. Statistical Parameters of Linear Correlations calculated mean vs experiment of pKa1 and pKa2

 dissociation constants of phosphonic acids

	pKa1	pKa2
$A\pm\Delta A$	-1.91±0.39	-0.80±0.94
$B\pm\Delta B$	2.01±0.16	1.08 ± 0.12
\mathbb{R}^2	0.91	086
SD	0.80	0.78
Ν	17	16
Without	14, 18, 19, 20, 21 and 24.	13, 15, 17, 18, 19, 20 and 22.

Indeed, from Table 1, it should be noted that the experimental values of pKa used in the correlations for compounds 14 and 16 were not measured by (Freedman, L.D, 1957). Their pKa values are from reference [D.E.C. Corbridge, Phosphorus: Chemistry, Biochemistry and Technology, Sixth Edition, p 379]. As for the pKa's halogenated compounds 18, 19, 20, 21 and 23, their pKa₁ values are certainly quite low one (pH unit) in view of the relatively stronger acidity because of halogen substituent. In addition, some pKa aliphatic compounds were deduced by extrapolation considering the number of carbon atoms.

To scale, the pKa1 constant of all R-PO₃H₂phosphonic acids including R=H, the pka₁ experimental values are compared to those of the corresponding R-COOH carboxylic acids. Table 7(appendix) lists the dissociation constant values with the relative difference Δ pKa. It is noted that the compounds 14, 18, 19, 20, 21, 22 and 23 have relatively, small deviations compared to those of aliphatic ones. The mean relative difference values (MRD) with and without these compounds are 1.73±0.95 and 2.21±0.54 pKa units respectively.

The scaled pKa's of phosphonic acids show good linear correlation with the corresponding pKa₁ mean values calculated at SMD-HF and B3LYP levels with R^2 value of 0.94 figure 7. However, the pKa₁ values of 18, 20 and 21 compounds are relatively underestimated. All the same, the MSE is reduced to 0.57 ± 1.85 with N=24 compounds versus -0.06 ± 1.03 pKa units without 18, 20 and 21 compounds.

IV. CONCLUSIONS

The relative pKa₁ and pKa₂ of 24 phosphonic acids in aqueous solution are carried out at SMD-HF/6-31⁺⁺G**//SMD-HF/6-31⁺⁺G**, SMD-HF/LANL2DZ//SMD-HF/LANL2DZ, SMD-B3LYP/6-31⁺⁺G**, SMD-B3LYP/LANL2DZ//SMD-HF/LANL2DZ.

The correlations between calculated pKa and experimental ones are of satisfactory quality.

The results obtained give confidence in the calculation methods and offer a means of predicting experimental pKa values for phosphonic acids, which present difficulties with experimental measurements.



Figure7: (a) Linear correlation between experimental dissociation constant values of phosphonic acids (pKa₁) and carboxylic acids (pKa). (b) Linear correlation between experimental scaled and calculated mean dissociation constant values of phosphonic acids.

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Supporting Information

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APPENDIX

	pKa ₁ and pKa ₂														
	Compounds	Cal	culated	values (t	this wo	rk)				Mean value	85	Literature			
N	R-PO(OH)2	HF/B1		HF/B2		B3LYP	/B1	B3LY	P/B2	pKa _i Cal±SD	pKa ₂ Cal±SD	Cal±SD [1]		[2]	
1	Hydrogene											2,00	6,58	1,30	6,70
2	Methyl	3,15	8,40	3,84	7,65	2,73	8,66	2,48	6,95	3.05±0.51	7.91±0.61	2,35	7,20	2,68	6,32
3	Ethyl	3,04	8,69	2,66	8,50	3,81	7,86	2,22	7,24	2.93±0.58	8.08±0.64	2,43	7,85	2,43	8,05
4	n-propyl	3,50	8,35	3,62	8,42	3,86	6,87	3,03	7,20	3.50±0.30	7.71±0.36	2,45	8,06	2,49	8,18
5	n-Butyl	3,61	8,37	2,90	8,37	4,18	7,53	2,16	6,99	3.21±0.76	7.82±0.63	2,59	8,19		
6	n-Hexyl	3,68	8,35	1,28	9,24	4,21	7,89	2,19	7,31	2.84±1.17	8.20±0.69	2,60	7,90		
7	isoPropyl	3,56	8,71	3,37	8,71	3,97	7,72	2,94	6,91	3.46±0.37	8.01±0.82	2,55	7,75	2,79	8,88
8	isoButyl	3,44	8,67	2,68	10,6 9	3,89	9,88	1,72	8,66	2.93±0.82	9.47±0.92	2,70	8,43		
9	s-butyl	3,61	8,84	2,60	8,64	4,16	7,91	2,62	6,63	3.25±0.66	8.00±0.96	2,74	8,48		
10	t-butyl	3,68	8,81	3,70	8,76	4,15	7,39	3,58	7,48	3.77±0.22	8.11±0.67	2,79	8,88		
11	neopentyl	4,48	8,74	3,23	8,88	4,74	8,13	2,67	8,55	3.78±0.86	8.57±0.19	2,84	8,65		
12	1,1- dimethylpropyl	3,54	8,79	3,16	8,87	3,97	7,34	2,63	6,69	3.32±0.49	7.92±0.99	2,88	8,96		
13	Benzyl	2,87	7,66	2,34	7,55	3,20	6,98	1,69	5,72	2.52±0.57	6.98±0.84	2,30	7,55	2,38	5,98
14	Ethenyl	2,53	7,58	1,41	7,54	2,72	7,19	1,09	5,77	1.94±0.70	7.02±0.78			3,48	8,55
15	2-phenylethenyl	2,48	7,70	1,85	7,63	2,59	6,58	1,34	5,86	2.06±0.51	6.94±0.84	2,00	7,10		
16	phenyl	1,42	7,12	1,58	8,17	2,27	7,54	1,54	3,94	1.70±0.33	6,69±1.59			2,05	5,51
17	methoxy	1,54	7,07	1,92	7,18	2,01	6,14	1,00	5,50	1.62±0.40	6.47±0.73	1,91	7,15		
18	trifluoromethyl	-5,24	1,16	-7,46	1,46	-4,30	- 2,68	- 7,98	- 2,45	- 6.25±1.52	-0.63±1.88	1,16	3,93	1,46	2,43
19	chloromethyl	-0,20	5,41	-1,29	5,85	0,13	4,10	- 1,51	3,61	- 0.72±0.70	4.74±0.92	1,40	6,30	1,70	5,22
20	dichloromethyl	-3,04	3,76	-3,71	4,05	-2,96	1,28	- 4,08	0,86	- 3.45±0.47	2.49±1.44	1,14	5,61		
21	trichloromethyl	-4,91	1,29	-6,79	1,68	-4,33	- 1,69	- 7,82	- 1,40	- 5.96±1.41	-0.03±1.44	1,63	4,81		
22	bromomethyl	0,55	6,38	-0,52	6,48	0,80	5,21	- 0,42	6,17	0.10±0.58	6.06±0.31	1,14	6,52		
23	iodomethyl	***	***	1,31	5,31	***	***	0,67	10,9 5	0.99±0.32	8.13±2.82	1,30	6,72		
24	trimethylsilano méthyl	***	***	2,40	8,92	***	***	1,18	8,20	1.79±0.61	8.56±0.36	3,22	8,60		

Table 1. Calculated pKa's at HF and B3LYP level using 6-31++G** (B1) and LANL2DZ (B2) basis set with SMD
Solvation model and Experimental data of the phosphonic acids.

	Compounds		∆pKal and ∆pKa2											
Ν	R-P(O)(OH)2	HF/B1		HF/B2		B3LYP	/B1	B3LYP/B2		Mean value		Exp		Ref
2	Methyl	0.80	1,20	1,49	0,45	0,38	1,46	0,13	-0,25	0,70	0,71	2,35	7,20	[1]
3	Ethyl	0.61	0,84	0,23	0,65	1,38	0,01	-0,21	-0,61	0,50	0,23	2,43	7,85	[1]
4	n-propyl	1.50	0,29	1,17	0,36	1,41	-1,19	0,58	-0,86	1,05	-0,35	2,45	8,06	[1]
5	n-Butyl	1.02	0,18	0,31	0,18	1,59	-0,66	-0,43	-1,20	0,62	-0,37	2,59	8,19	[1]
6	n-Hexyl	1.08	0,45	-1,32	1,34	1,61	-0,01	-0,41	-0,59	0,24	0,30	2,60	7,90	[1]
7	isoPropyl	1.01	0,96	0,82	0,96	1,42	-0,03	0,39	-0,84	0,91	0,26	2,55	7,75	[1]
8	isoButyl	0.47	0,24	-0,02	2,26	1,19	1,45	-0,98	0,23	0,23	1,04	2,70	8,43	[1]
9	s-butyl	0.87	0,36	-0,14	0,16	1,42	-0,57	-0,12	-1,85	0,51	-0,48	2,74	8,48	[1]
10	t-butyl	0.89	-0,07	0,91	-0,12	1,36	-1,49	0,79	-1,40	0,98	-0,77	2,79	8,88	[1]
11	néopentyl	1.64	0,09	0,39	0,23	1,90	-0,52	-0,17	-0,10	0,94	-0,08	2,84	8,65	[1]
12	l,l dimethylpropyl	0.66	-0,17	0,28	-0,09	1,09	-1,62	-0,25	-2,27	0,44	-1,04	2,88	8,96	[1]
13	Benzyl	0.57	0,11	0,04	0,00	0,90	-0,57	-0,61	-1,83	0,22	-0,57	2,30	7,55	[1]
14	Ethenyl	-0.95	-0,97	-2,07	-1,01	-0,76	-1,36	-2,39	-2,78	-1,54	-1,53	3,48	8,55	[2]
15	2-phenylethenyl	0.48	0,60	-0,15	0,53	0,59	-0,52	-0,66	-1,24	0,06	-0,16	2,00	7,10	[1]
16	phenyl	-0.63	1,61	-0,47	2,66	0,22	2,03	-0,51	-1,57	-0,35	1,18	2,05	5,51	[2]
17	methoxy	-0.37	-0,08	0,01	0,03	0,10	-1,01	-0,91	-1,65	-0,29	-0,68	1,91	7,15	[1]
18	trifluoromethyl	-6.40	-2,77	-8,62	-2,47	-5,46	-6,61	-9,14	-6,38	-7,41	-4,56	1,16	3,93	[1]
19	chloromethyl	-1.60	-0,89	-2,69	-0,45	-1,27	-2,20	-2,91	-2,69	-2,12	-1,56	1,40	6,30	[1]
20	dichloromethyl	-4.18	-1,85	-4,85	-1,56	-4,10	-4,33	-5,22	-4,75	-4,59	-3,12	1,14	5,61	[1]
21	trichloromethyl	-6.54	-3.52	-8,42	-3,13	-5,96	-6,50	-9,45	-6,21	-7,59	-4,84	1,63	4,81	[1]
22	bromomethyl	-0.59	-0.14	-1,66	-0,04	-0,34	-1,31	-1,56	-0,35	-1,04	-0,46	1,14	6,52	[1]
23	iodomethyl			0,01	-1,41			-0,63	2,50	-0,31	1,41	1,30	6,72	[1]
24	trimethylsilano méthyl			-0,82	0,32			-2,04	-0,40	-1,43	-0,04	3,22	8,60	[1]

 Table 2. Errors (ΔpKa) mean signed errors (ME), mean unsigned errors and standard deviation (SD) in pKa's of phosphonic acids calculated at SMD-HF and SMD-B3LYP.

	Substituent	P	pKaexperimental ΔpKa			pKa _i (RPC	∆pKa	
N°	Name	R	RCOOH (ref)	RPO ₃ H ₂	(Exp-Exp)	Scaled	Calculated	(Scal-Calc)
1	Hydrogene	Н	3,77 (Riddick J.A,1985)	1,30	2,47	1,84	1,3	0,54
2	Methyl	CH3	4,76 (Serjeant, E.P, 1979)	2,35	2,41	2,54	3,05	-0,51
3	Ethyl	C2H5	4,88 (Serjeant, E.P, 1979)	2,43	2,45	2,62	2,93	-0,31
4	n-propyl	C3H7	4,82 (Riddick J.A,1985)	2,45	2,37	2,58	3,5	-0,92
5	n-Butyl	C4H9	4,84 (Dean, J.A, 1987)	2,59	2,25	2,61	3,21	-0,6
6	n-Hexyl	C6H13	4,89 (Dean, J.A, 1987)	2,60	2,29	2,63	2,84	-0,21
7	isoPropyl	(CH3)2CH	4,84 (Kortum G, 1961)	2,55	2,29	2,6	3,46	-0,86
8	isoButyl	(CH3)2CHCH2	4,77 (Kortum G, 1961)	2,70	2,07	2,55	2,93	-0,39
9	s-butyl	CH3-CH2CH(CH3)	4,97 (Dean, J.A, 1987)	2,74	2,23	2,69	3,25	-0,56
10	t-butyl	(CH3)3-C	5,03 (Dean, J.A, 1987)	2,79	2,24	2,73	3,77	-1,05
11	neopentyl	(CH3)3-C-CH2	4,79 [6]	2,84	1,95	2,56	3,78	-1,22
12	t-amyl	C2H5(CH3)2C	NA	2,88		2,88	3,32	-0,44
13	Benzyl	C6H5-CH2	4,31 (Haynes, W.M. 2015)	ynes, W.M. 2015) 2,30 2,		2,22	2,52	-0,3
14	Ethenyl or vinyl	CH2=CH	4,25 (Riddick J.A, 1985) 3,48		0,77	2,18	1,94	0,24
15	2-phenylethenyl	C6H5-CH=CH	4,44 [8] 2,00		2,44	2,31	2,06	0,25
16	phenyl	C6H5	4,2 (Haynes, W.M, 2011)	1) 2,05 2,15		2,14	1,7	0,44
17	methoxy	HOCH2	3,83 (Serjeant, E.P, 1979)	1,91	1,92	1,79	1,62	0,17
18	trifluoromethyl	CF3	0,3 (O'Neil, MJ, 2001)	1,16	-0,86	-0,47	-6,25	5,78
19	chloromethyl	CH2C1	2,86 (Dean, J.A, 1999)	1,40	1,46	1,19	-0,72	1,91
20	dichloromethyl	CHC12	1,26 (Dean, J.A, 2000)	1,14	0,12	0,08	-3,45	3,53
21	trichloromethyl	CC13	0,52 (Dean, J.A, 2001)	1,63	-1,11	-0,38	-5,96	5,58
22	bromomethyl	CH2Br	2,86 (Brown, H. C, 1955)	1,14	1,72	1,19	0,1	1,09
23	iodomethyl	CH2I	3,18 (Lide, DR , 2000)	1,30	1,88	1,38	0,99	0,39
24	trimethylsilanomethyl	(CH3)3-Si-CH2	5,22 (Colvin, E, 1981)	3,22	2,00	2,87	1,79	1,08
		mean relative differ	rence (MRD)		1,73	MSE		0.57
		standard deviat	tion (SD)		0,95	SD		1.85
		Without 14, 18,	19, 20, 21, 22 and 23.			1	Without 18, 2	0 and 21.
		mean relative differ	rence (MRD)		2,21	MSE		-0.06
		standard deviat	tion (SD)		0,53	SD		1.03
					-	-	-	

Table 3: Relative difference (Δ pKa), mean relative difference (MRD), standard deviation (SD) of pKa₁ values of phosphonic acids compared to pKa of carboxylic acids. Δ pKa(Exp-Exp)= pKa(RCOOH)-pKa₁(RPO₃H₂), and Δ pKa(Scal-Calc) = pKa1(scaled)-pKa₁(calc.), and errors (Δ pKa₁), mean signed errors (MSE), and standard deviation (SD) in calculated pKa's of phosphonic acids at SMD-HF and SMD-B3LYP